In Situ Transmission X-Ray Microscopy of the Lead Sulfate Film Formation on Lead in Sulfuric Acid

K. W. Knehr,^{a,*} Christopher Eng,^b Yu-chen Karen Chen-Wiegart,^{b,**} Jun Wang,^b and Alan C. West^{a,**}

^aDepartment of Chemical Engineering, Columbia University, New York, New York 10027, USA

^bPhoton Sciences Directorate, Brookhaven National Laboratory, Upton, New York 11973, USA

Transmission X-ray microscopy is utilized to monitor, in real time, the behavior of the PbSO₄ film that is formed on Pb in H₂SO₄. Images collected from the synchrotron x-rays are coupled with voltammetric data to study the initial formation, the resulting passivation, and the subsequent reduction of the film. It is concluded with support from quartz-crystal-microbalance experiments that the initial formation of PbSO₄ crystals occurs as a result of acidic corrosion. In addition, the film is shown to coalesce during the early stages of galvanostatic oxidation and to passivate as a result of morphological changes in the existing film. Finally, it is observed that the passivation process results in the formation of large PbSO₄ crystals with low area-to-volume ratios, which are difficult to reduce under both galvanostatic and potentiostatic conditions.

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Manuscript submitted September 23, 2014; revised manuscript received November 10, 2014. Published December 9, 2014.

Lead-acid batteries have been a major part of the economy for over 100 years.¹ Recently, they have seen significant use in next-generation energy storage applications (e.g., renewable energy storage, smart-grid buffering, and transportation) due to their high energy efficiency (up to 80%), low capital cost, and the existence of a strong manufacturing, distribution, and recycling infrastructure.² During discharge of a lead-acid battery, Pb is transformed into PbSO₄ at the surface of the negative electrode through the following reaction with H₂SO₄:

As a result of the reaction, the Pb electrode is coated by a PbSO₄ film, which is reduced during charge. The performance and life-time of lead-acid batteries is greatly affected by the formation, growth, and resulting morphology of the PbSO₄ film.³ For instance, one of the major factors limiting the lifetime of lead-acid batteries in high-rate, partial state-of-charge applications (i.e., electric and hybrid-electric vehicles) is the progressive sulfation of the negative electrode, whereby the PbSO₄ film becomes irreversible and cannot be fully converted back into Pb after a sufficient charge.^{4,5}

In the past 40 years, there has been a considerable effort focused on the formation of the PbSO₄ film; however, there is still no general consensus on the exact mechanisms of nucleation and growth. For instance, both the Lakeman and Harrison groups studied the mechanisms of PbSO₄ formation and suggested a dissolution-precipitation mechanism at low overpotentials with solid-state nucleation-and-growth occurring at high overpotentials.^{6–11} Later work by Hall and Wright, which was further developed by Varela et al., suggested that both mechanisms (dissolution-precipitation and solid-state nucleation-and-growth) occur simultaneously in a complex manner which results in a bi-layered salt film with different properties for each layer. They suggested that passivation resulted from large crystals forming on top of a porous film as a result of a dissolution-precipitation mechanism.^{12–14} More recently, Yamaguchi et al. have concluded that only a single layer of PbSO₄ forms as a result of a dissolution-precipitation mechanism and that sulfation may result from the chemical re-crystallization of electrochemically formed PbSO₄.¹⁵

Most of the early studies on PbSO₄ formation relied on the interpretation of voltammetric data to indirectly understand the formation processes on Pb. Potentiostatic pulses and voltammetric sweeps were applied to the electrode, while the resulting current responses were measured and analyzed. Later, attempts were made to provide visual evidence by combining the same voltammetric techniques with

atomic force microscopy (AFM). The AFM studies were able to obtain valuable information on the effects of operating conditions (e.g., open circuit standing time and cyclic voltammetry sweep rate) and the impact of electrolyte additives on the size and growth rates of the PbSO₄ crystals.^{15–20} Further advancement of this in situ work would require a new technique that overcomes the small viewing window (25 to 100 μm²) and slow acquisition time (52 sec per image) associated with AFM. A larger viewing window and a faster acquisition rate would make it possible to capture inhomogeneities in crystal formation and to better quantify growth. In addition, these experiments could be further improved through the use of constant current (galvanostatic) operating conditions. Electrochemical testing of full scale battery systems is typically done using constant current cycling at variable C-rates.^{21–23} Therefore, a fundamental understanding of PbSO₄ growth under these conditions could yield valuable information which can be directly related to lead-acid battery performance. In particular, this understanding could help to further identify methods for significantly reducing irreversible or hard sulfation.

This work seeks to elucidate the mechanisms of PbSO₄ film formation on Pb in H₂SO₄ using in situ transmission X-ray microscopy (TXM). TXM is a newly developed imaging technique with a large field of view (1600 μm²), which is capable of producing X-ray micrographs at fast acquisition rates (up to one second time intervals) and with sub-40 nm resolutions. The formation, growth, and reduction of PbSO₄ on Pb in H₂SO₄ are monitored, in real time, under potentiostatic and galvanostatic operating conditions. In addition, quartz-crystal-microbalance experiments are conducted to support the voltammetric and visual data collected from the TXM. In the following sections, the in situ set-up is presented along with an investigation of the initial growth, passivation, and reduction of the PbSO₄ film.

Experimental

Cell design.— The visualization of the growth and reduction of PbSO₄ on Pb with synchrotron X-rays was made possible with the use of an in-house designed, in situ, micro-electrochemical cell. The design of the cell is shown in Figure 1. The Pb electrode was formed by sputter coating a 20-nm thick strip of Au/Pd on top of a translucent PET film (Fig. 1, part iv). Next, a 0.5-μm thick layer of Pb was electroplated on the Au/Pd strip using a Pb-plating bath continuously stirred at 200 rpm and consisting of 375 g/L lead fluoborate, 22.5 g/L fluoboric acid, 30 g/L boric acid, and 5.3 g/L peptone.²⁴ The plating was conducted at a constant current density of −18 mA cm^{−2} in a two-electrode system. A solid Pb sheet with a surface area that is 10× greater than the cathode area served as the counter electrode.

*Electrochemical Society Student Member.

**Electrochemical Society Active Member.

[†]E-mail: kwk2111@columbia.edu

Figure 1. Design of in situ, micro-electrochemical cell used to monitor PbSO_4 growth on Pb using synchrotron x-rays.

After plating, the PET film was rinsed with de-ionized water, dried with compressed air, and immediately assembled into the in situ cell.

In the cell, the electrochemically active area (0.18 cm^2) was defined using a silicon gasket (Fig. 1, part iii), which was sandwiched between two PET films (Fig. 1, parts ii and iv). The gasket was 127 μm thick (before compression) and, along with defining the active area, also provided a channel for the H_2SO_4 . The electrical connection was made to the Pb electrode by a 38- μm thick copper strip that was placed in between the gasket and the Pb (Fig. 2c). The whole cell was held in place by two polycarbonate braces, which were bolted together. Each brace contained a hollow window to provide a path for the synchrotron X-rays, which were only transmitted through the PET films, H_2SO_4 , and Pb. One of the braces and the PET film without

the Pb also contained inlet/outlet holes for the electrolyte (Fig. 1, parts i and ii). The polycarbonate brace (Fig. 1, part i) was fitted with landings for connection to tubing.

TXM set-up and procedure.— During the experiment, the in situ cell was positioned in the transmission X-ray microscope with the X-ray beam penetrating through the Pb in a direction normal to the surface (Fig. 2a). Using flow tubes, the top of the in situ cell was connected to an external cell, which was placed outside of the beam flight-path. A $\text{Hg}|\text{Hg}_2\text{SO}_4$ reference electrode in 4.6 M H_2SO_4 and a platinum counter electrode were placed inside the external cell (Fig. 2b). A syringe was connected to the bottom of the in situ cell and used to fill the entire system with H_2SO_4 . The experiment was conducted with 4.6 M H_2SO_4 , which was deaerated for 3 hours with argon gas.

The electrochemical growth and reduction of the film was controlled using a BioLogic VMP3 potentiostat, which was connected to all three electrodes – the lead electrode in the in situ cell and the reference and counter electrodes in the external cell. Prior to the experiment, galvanostatic electrochemical impedance spectroscopy (EIS) was conducted with a bias current equal to 0 μA , a frequency range from 10 kHz to 100 mHz, and an amplitude of $\pm 10\text{ }\mu\text{A cm}^{-2}$. The inherent ohmic resistance of the setup (3466 Ω) was determined from the high frequency intercept on the real axis of the Nyquist plot.²⁵ This value was used to correct for ohmic drop between the reference and Pb electrodes (i.e., iR compensation) during the galvanostatic experiments. The full experimental procedure (without the EIS) is described in Figure 3, which includes the current and voltage of the system. All times in the remaining figures throughout the paper are reported in reference to Figure 3. To start the experiment, the Pb was first held at constant voltages of -1.1 V and -1.2 V for 30 minutes (regions ‘a’ and ‘b’) in order to reduce any PbSO_4 that formed on the Pb while sitting in H_2SO_4 . Next, the working electrode was held at the open-circuit voltage (OCV) for 2 minutes (region ‘c’), followed by a galvanostatic oxidation (region ‘d’) at $50\text{ }\mu\text{A cm}^{-2}$ with a cut-off voltage of -0.87 V (-0.84 V before correcting for ohmic drop). During the oxidation, PbSO_4 was formed on Pb. After reaching the cutoff voltage, the Pb was held at OCV for 2 minutes (region ‘e’) and then galvanostatically reduced (region ‘f’) at $-50\text{ }\mu\text{A cm}^{-2}$ with a cutoff voltage of -1.17 V (-1.2 V before correcting for ohmic drop). Finally, a potentiostatic reduction was performed for 30 minutes at -1.1 V (region ‘g’) in an attempt to reduce all the remaining PbSO_4 back to Pb.

Figure 2. Experimental set-up for the in situ, electrochemical experiments. a) Placement of the in situ, micro-electrochemical cell in the TXM at Brookhaven National Laboratory. b) Image of the experimental system (i.e., syringe, in situ cell, and external cell) outside of the TXM. c) Close-up image of the in situ cell.

Figure 3. Voltage and current data during in situ experiment. Description of regions: (a) -1.1 V for 30 min; (b) -1.2 V for 30 min; (c) OCV for 2 min; (d) oxidation at $50\text{ }\mu\text{A cm}^{-2}$ with a cut off voltage of -0.87 V ; (e) OCV for 2 min; (f) reduction at $-50\text{ }\mu\text{A cm}^{-2}$ with a cut off voltage of -1.17 V ; (g) -1.1 V for 30 min.

Figure 4. Processing of image taken at $t = 62$ min: (a) original image, (b) difference with Pb background (i.e., image taken at $t = 60$ min), (c) contrast correction, (d) pixel outlier removal.

Transmission X-ray microscopy.— The in situ transmission X-ray microscopy (TXM) was done at the X8C beamline of the National Synchrotron Light Source at Brookhaven National Laboratory. TXM is a non-destructive, nanoscale resolution, highly penetrative hard X-ray imaging technique in which the sample environment can be easily controlled via the development and implementation of in situ environmental apparatuses.²⁶ In situ imaging was done at an X-ray energy of 8 keV with a large $40 \times 40 \mu\text{m}$ ($1600 \mu\text{m}^2$) field of view and an exposure time of 20 seconds for each image. The moderate exposure time made it possible to generate a clear image by binning a 2×2 pixel region using the $2k \times 2k$ CCD camera, resulting in a pixel size of 39 nm. At the start of the in situ experiment, five background images were collected of the lead sample and used for pixel-by-pixel normalization. Figure 4a shows an example of a TXM image after normalization. The image was taken during the galvanostatic oxidation at $t = 62$ minutes.

Additional refinement of the in situ images was done using ImageJ software in order to better visualize the nucleation and growth processes of the PbSO_4 film.²⁷ In light of this additional processing, TXM images which were only altered through normalization with the Pb background are considered un-processed. Figure 4 shows the three-step refinement process for a single TXM image. In the first step, an image calculator is used to take the pixel-by-pixel difference of the 8-bit grayscale values of two images: the image in question (Fig. 4a) and an un-processed image of pure Pb taken during OCV at $t = 60$ minutes into the experiment. The difference operator removes background features and enhances the PbSO_4 crystals, as shown in Figure 4b. For the next step, a contrast adjustment is performed on the image by setting the maximum 8-bit gray scale value to 100 and adjusting the respective pixel lookup tables (Fig. 4c). Finally, a pixel outlier removal operation is performed for both dark and bright outliers, which uses a pixel radius of two and an 8-bit grayscale threshold of 50.²⁸ The final, processed image after all three steps is shown in Figure 4d.

Quartz crystal microbalance.— The quartz-crystal-microbalance (QCM) experiment was conducted using a PLO-10i phase lock oscillator (Maxtex, Inc.) equipped with a Teflon crystal holder (model no. CHC-100). The experiment employed a 5 MHz AT-cut, polished

quartz crystal, and the resonance frequency from the crystal was monitored using a Hewlett-Packard 53131A frequency counter.²⁹ The initial electrode was comprised of a platinum coating on top of a titanium seed layer. In order to obtain a Pb electrode, a $10\text{-}\mu\text{m}$ thick layer of Pb was electrodeposited on top of the platinum electrode using the plating procedure previously described herein. The constant current plating was controlled using a $\mu\text{AutolabIII}$ potentiostat (Metrohm USA, Inc.), and the electrode was contained in the Teflon holder. After plating, the quartz crystal was removed from the Teflon holder, rinsed with deionized water, and dried with nitrogen gas. The quartz crystal was then placed back in the holder and submersed in 100 mL of 4.6 M H_2SO_4 for the QCM experiment. The H_2SO_4 was purged with argon gas for 3 hours prior to the experiment. Along with the Pb coated quartz crystal, the QCM set-up included a $\text{Hg}|\text{Hg}_2\text{SO}_4$ reference electrode in 4.6 M sulfuric acid to monitor the voltage and a platinum counter electrode.

Results and Discussion

TXM results.—potentiostatic reductions.— Figure 5 shows the results of the potentiostatic reductions at -1.1 V and -1.2 V, which were performed at the beginning of the TXM experiment (Fig. 3, regions ‘a’ and ‘b’). Each numbered point on the voltage curve corresponds to the time the respective image was taken. The objective of these procedures was to remove any PbSO_4 film that had grown on the Pb surface during the five-minute period between filling the in situ, micro-electrochemical cell with H_2SO_4 and the start of the experiment. Image 1, in Figure 5, shows the presence of a surface film at the start of the experiment. A similar film was observed by Yamaguchi et al. for a Pb electrode immersed in 0.05 M H_2SO_4 for 20 minutes using AFM.²⁰ There are two possible mechanisms for the formation of the initial PbSO_4 film. First, dissolved oxygen present in the electrolyte could form PbSO_4 through the following reaction:^{3,30}

Due to the fast kinetics of the electrochemical reduction of oxygen on the Pb electrode, the reaction in Eq. 2 is diffusion-limited, i.e. the reaction rate is controlled by the mass transfer of oxygen to the Pb surface.³¹ Therefore, any oxygen present near the electrode will readily cause the formation of PbSO_4 . Despite the fast kinetics of the oxygen reaction, this mechanism is unlikely since the electrolyte in the current study was deaerated with argon before the experiment. Therefore, the film was most likely formed as a result of acid corrosion via the following reaction:^{3,30}

According to the potential vs. pH (Pourbaix) diagram for the Pb/ H_2SO_4 system, the corrosion reaction in Eq. 3 is thermodynamically unavoidable at the low pH of the 4.6 M H_2SO_4 .¹

Despite the initial presence of the film, images 2–5 in Figure 5 clearly depict that the constant potential procedures succeed in reducing the film to bare Pb. The majority of the surface film is reduced during the first 12 minutes at -1.1 V (Fig. 5, image 3), and all but a few crystals remain after 30 minutes (Fig. 5, image 4). Although most of the PbSO_4 is consumed within 30 minutes, there is still a constant cathodic current, which can be attributed to hydrogen evolution on the surface of the Pb. At $t = 60$ minutes into the experiment (Fig. 5, image 5), no surface film is present, providing a clean Pb sample as a starting point for the remainder of the TXM experiment.

OCV and galvanostatic oxidation.—In order to investigate the nucleation and growth of the PbSO_4 film, after the potentiostatic reduction step, the Pb electrode was held at OCV for two minutes and then oxidized at a constant current density of $50 \mu\text{A cm}^{-2}$. The voltage response and resulting TXM images of the OCV and initial oxidation can be found in Figure 6. The numbered regions on the voltage vs. time graph indicate the exposure time for each image. From image 2 of the figure, it appears that the nucleation of PbSO_4 crystals starts before the oxidation current is applied, indicating that the initial

Figure 5. Current response of potentiostatic reductions (regions 'a' and 'b' in Fig. 3) and corresponding, un-processed TXM images.

formation of PbSO_4 is due to an electrochemical corrosion reaction. The previously described acidic corrosion of Pb (Eq. 3) is most likely responsible for the initial nucleation. Image 2 also indicates that the onset of the corrosion reaction is rapid, with crystals up to 1 μm in diameter visible 1.5 minutes into the open-circuit voltage measurement. For a lead-acid battery at OCV, this rapid corrosion will occur on the negative electrode and has been shown to decrease the capacity of the electrode at rates of up to 0.5% per day.³²

Figure 6 also makes it possible to monitor the growth of the film. After the nucleation process, the film continues to grow, coating the Pb surface as it spreads out from the initial nucleation sites. In addition to the spreading of the film, a comparison of images 2 and 3 indicates an increase in the total number of PbSO_4 crystals during growth. This suggests that PbSO_4 crystals are constantly formed during the growth process, which would correspond to progressive

nucleation. It is important to note that an increase in total crystals was observed for all images between $t = 61.5$ to 63 minutes. Therefore, the increase in crystals between images 2 and 3 was not a result of the application of an oxidation current, but a demonstration of the consistent formation of nuclei. This fact is clearly shown in Figure 7, where the crystal densities from several TXM images are plotted as a function of time. These observations of a progressive nucleation are in contradiction with the findings of several authors who have interpreted chronoamperometry and concluded that the film forms as a result of an instantaneous nucleation process.¹¹⁻¹³ This discrepancy may be due to the fact that the previous nucleation and growth studies are typically reported for high anodic overpotentials (>50 mV) where solid-state reactions are assumed to dominate. The present oxidation occurs at low anodic overpotentials (<20 mV) where a dissolution-precipitation mechanism is thought to occur.⁷

Figure 6. Voltage response of open-circuit voltage and initial stage of galvanostatic oxidation (regions 'c' and 'd' in Fig. 3, respectively) and corresponding TXM images.

Figure 7. Lead sulfate crystal density at end of OCV and start of galvanostatic oxidation (regions 'c' and 'd' in Fig. 3, respectively). $R^2 = 0.98$.

These conclusions suggest that the progressive nucleation of PbSO_4 observed in Figs. 6 and 7 results from a dissolution-precipitation mechanism.

At $t = 64.5$ minutes (Fig. 6, image 5), the film is fully coalesced, and the Pb electrode is completely covered by PbSO_4 . This occurs three minutes after the first PbSO_4 crystal is observed (Fig. 6, image 2), and indicates that the Pb electrode is fully covered during the early stages of the oxidation experiment. Figure 8 shows the voltage response of the complete oxidation and the resulting TXM images. As a point of reference, image 1 in Figure 8 and image 3 in Figure 6 are the same image. In this experiment, the passivation of the electrode, as indicated by the rapid increase in anodic voltage, occurs at $t = 102$ minutes. A cutoff voltage of -0.87 V was used to indicate the end of PbSO_4 oxidation and to prevent the formation of PbO compounds at higher anodic potentials.³³ Since the PbSO_4 film fully covers the Pb electrode several minutes into the process, the majority of the galvanostatic oxidation (97.5% of the total time) corresponds to the growth of a pre-existing, fully coalesced film (Fig. 8, images 2 to 5). The passivation (image 5) can, therefore, be attributed to mor-

phological changes in the PbSO_4 film which impede the oxidation process. Earlier authors have suggested that passivation is caused by a thickening or reduction in porosity of the film, which restricts the mass transport of ions (Pb^{2+} or SO_4^{2-}) to the reaction sites at or near the Pb surface.^{34,35} The TXM images in the present study support this conclusion.

Reduction of the PbSO_4 film.—After the completion of the galvanostatic oxidation, a galvanostatic reduction (Fig. 3, region 'f') was conducted at $-50 \mu\text{A cm}^{-2}$ in an attempt to reduce the passivating PbSO_4 film back to Pb. A cutoff voltage of -1.17 V was used to indicate the end of PbSO_4 reduction and to prevent excess gassing of hydrogen at the electrode. The voltage curve in Fig. 3 shows that the reduction of PbSO_4 back to Pb is a rather inefficient reaction, with the reduction reaching the cutoff voltage in less than five minutes. The low efficiency can be attributed to the high applied current density, which caused the cutoff voltage to be reached before all the PbSO_4 was reduced. Ekdunge et al. have shown that the diffusion and/or dissolution of Pb^{2+} ions are the rate-determining steps during the reduction of the PbSO_4 electrode.³⁶ It is possible that the applied current quickly exceeded the rates of these processes, causing a rapid increase in the overpotential in order to generate current via hydrogen evolution. A more complete reduction would be expected at lower current densities. By comparing the times of the galvanostatic reduction and oxidation procedures, it is reasonable to assume that up to 88% of the PbSO_4 formed on the electrode surface during the galvanostatic oxidation remains at the end of the galvanostatic reduction. In an attempt to further reduce this excess film, a potentiostatic reduction of -1.1 V was applied to the Pb electrode immediately after the galvanostatic reduction (Fig. 3, region 'g').

Figure 9 shows the current response of the -1.1 V potentiostatic reduction and the subsequent TXM images taken at the beginning and end of the technique. These images were only altered through normalization with the Pb background and were not processed with the ImageJ software. Image 1 shows the existence of well-defined PbSO_4 crystals up to $4 \mu\text{m}$ in diameter, which remained on the Pb surface at the end of the galvanostatic experiments. At the end of the potentiostatic reduction, these crystals appear to have shrunk in size but still remain on the surface (image 2). These images can be compared to those obtained during the potentiostatic reductions at the beginning of the experiment (Fig. 5). The PbSO_4 crystals formed during the TXM experiment persist longer than those formed at open-circuit voltage. This is most likely due to the fact that the PbSO_4 crystals in Fig. 9

Figure 8. Voltage response of galvanostatic oxidation (region 'd' in Fig. 3) and corresponding TXM images.

Figure 9. Current response of potentiostatic reduction performed after galvanostatic experiments (region 'g' in Fig. 3) and un-processed, TXM images before and after technique.

are much larger than those in Fig. 5, and therefore, they have a lower area-to-volume ratio. The lower surface area impedes the dissolution of the PbSO_4 , which is the first step in the reduction of the film.³⁶ Although the same potential of -1.1 V is applied to the electrode at the start (Fig. 3, region 'a') and end of the experiment (Fig. 3, region 'g'), the current obtained from the electrode differs due to changes in PbSO_4 crystal morphology. Similar results have been observed by Kanamura and Takehara, who were able to model the effects of crystal size on the reduction current obtained from cyclic voltammograms.³⁷

In addition, image 2 (Fig. 9) shows that the spaces between the large crystals appear to have brightened during the potentiostatic reduction, which corresponds to an increase in X-ray transmission through the sample. The increase in transmission can be attributed to the reduction of the PbSO_4 film. The brightened area in image 2 is most likely the bare, Pb electrode which is exposed as a result of the PbSO_4 reduction. Because no distinct crystals are observed in this region in image 1, the film between the large crystals most likely consists of smaller crystals whose morphology is indistinguishable using the TXM. This suggests that, while it was difficult for the large crystals to reduce, smaller PbSO_4 crystallites were reduced.^{5,38} The existence of large and small crystals can be associated with the progressive nucleation of PbSO_4 observed in Figures 6 and 7. The constant formation of new nuclei results in crystals of different sizes. An easily reduced PbSO_4 film would be preferred in order to maximize the efficiency and to maintain the capacity of a lead-acid battery.

Quartz crystal microbalance.— In order to support the claims made herein of a high acidic corrosion rate for Pb in H_2SO_4 , quartz crystal microbalance (QCM) experiments were performed. A QCM is able to detect small changes in mass on top of a quartz crystal by measuring the associated change in resonant frequency of the crystal. Sauerbrey was the first to recognize that the change in frequency of a quartz crystal can be directly related to the added mass through the following equation:³⁹

$$\Delta f = -C_f \times \Delta m \quad [4]$$

where Δf is the change in frequency, Δm is the change in mass per unit area, and C_f is a sensitivity factor, which is a fundamental

property of the quartz crystal. It is defined as follows:

$$C_f = \frac{\alpha 2 f_0^2}{\sqrt{\rho_q \mu_q}} \quad [5]$$

where f_0 is the resonant frequency of the unloaded crystal, ρ_q is the density of quartz, μ_q is the elastic shear modulus of quartz, and α is a dimensionless instrument constant.²⁹ For the current set-up, $C_f = 0.0566 \text{ Hz cm}^2 \text{ ng}^{-1}$.

In these experiments, a quartz crystal plated with a $10\text{-}\mu\text{m}$ thick film of Pb was placed in $4.6 \text{ M H}_2\text{SO}_4$, and the change in mass per unit area was monitored over time. A $\text{Hg}|\text{Hg}_2\text{SO}_4$ reference electrode was used to monitor the open circuit voltage, and it was confirmed that the electrode was near the reversible Pb/PbSO₄ potential. Figure 10a shows the recorded mass change per unit area over a 30 minute period. Also included in the figure is the mass change per unit area detected by Taguchi et al. for a Pb electrode in $4.5 \text{ M H}_2\text{SO}_4$ using the same technique.⁴⁰ Good agreement is observed between the two experiments. Both show a sharp initial rise in mass, which reaches a steady state ~ 10 minutes into the experiment. In order to compare the rate of corrosion with the oxidation rate used in the experiment, the mass change per unit area was converted into a corrosion current (i_{corr} [=] $\mu\text{A cm}^{-2}$). To accomplish this, the relative quantity of charge stored in the growing PbSO_4 film was determined from the change in measured mass per unit area using the following equation:

$$Q = \frac{nF\Delta m}{MW_{\text{SO}_4^{2-}}} \quad [6]$$

where F is Faraday's constant, n is the number of e^- passed per mole of SO_4^{2-} reacting, $MW_{\text{SO}_4^{2-}}$ is the molecular weight of SO_4^{2-} , and Q has units of C cm^{-2} . This equation assumes that all the PbSO_4 products remained on the surface, which is a reasonable assumption due to the low solubility of PbSO_4 in H_2SO_4 .⁴¹

Once the change in the quantity of charge (Q) was determined using Eq. 6, i_{corr} was calculated from the first order derivative of the quantity of charge with respect to time:

$$i_{\text{corr}} = \frac{dQ}{dt} \quad [7]$$

Figure 10. a) Mass change of Pb in H_2SO_4 determined using a quartz-crystal-microbalance. b) Corrosion rate calculated from slope of QCM results shown in (a).

Figure 10b depicts the change in i_{corr} over the 30 minute experiment. After a high initial value, i_{corr} appears to settle at a value equivalent to $50 \mu\text{A cm}^{-2}$. This is the same value used for the galvanostatic oxidation and reduction experiments performed in the TXM. It indicates that the acidic corrosion of Pb in H_2SO_4 is quite fast and is responsible for the nucleation of PbSO_4 crystals observed during the open-circuit voltage measurements.

Conclusions

This work presents an investigation of the surface behavior of the Pb/ PbSO_4 electrode in a lead-acid battery. In situ transmission X-ray microscopy was used to monitor, in real time, the formation, growth, and reduction of PbSO_4 on Pb in H_2SO_4 under potentiostatic and galvanostatic operating conditions. The resulting TXM images were used to show that the initial nucleation of PbSO_4 crystals occurred while the Pb electrode was held at an open-circuit voltage. Using a quartz-crystal microbalance, it was shown that this behavior could be attributed to the acidic corrosion of Pb in H_2SO_4 .

During the early stages of film formation, TXM images depicted a progressive nucleation of PbSO_4 crystals, which were concluded to form through a dissolution-precipitation mechanism. The data also showed that the PbSO_4 film was fully coalesced across the surface of the Pb electrode during the early stages of the galvanostatic oxidation. Therefore, it was concluded that the passivation of the electrode was due to morphological changes in the existing PbSO_4 film, which impeded the mass transport of reactants. In addition, the passivating film was shown to be stable and difficult to reduce. This behavior was attributed to the formation of a significant number of large crystals with low area-to-volume ratios, which hindered the dissolution of PbSO_4 .

Acknowledgments

K. W. K. greatly acknowledges the support of the National Science Foundation Graduate Research Fellowship under grant No. 1144155. Any opinions, findings, and conclusions or recommendations expressed in this material are those of the authors and do not necessarily reflect the views of the National Science Foundation.

This work was supported in part by the American Recovery and Reinvestment Act funding through Department of Energy, Office of Science, Office of Basic Energy Sciences. Use of the National Synchrotron Light Source, Brookhaven National Laboratory for this work was supported by the U.S. Department of Energy, Office of Science, Office of Basic Energy Sciences under Contract No. DE-AC02-98CH10886.

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